

Corso di Linguaggi di Programmazione: Modulo 1

Esercitazione in classe di fine modulo (n.1)

1) Sia B_{exp} l'insieme delle espressioni booleane generate dalla seguente sintassi astratta in BNF

$B ::= \text{true} \mid \text{false} \mid a \mid \sim B \mid B \text{ and } B$

Definire le regole di semantica operazionale strutturata secondo la strategia di valutazione "Esterna Sinistra". (N.B: a è una variabile booleana, ovvero che può assumere valore true o false in uno store σ ; di store ce ne possono essere solo 2, ovvero $\{(a, \text{true})\}$ e $\{(a, \text{false})\}$).

2) Mostrare che la grammatica al punto 1) è ambigua.

3) Disambiguare la grammatica al punto 1), assumendo che l'operatore di negazione \sim lega di più di (ovvero abbia precedenza su) and, e che and associ a sinistra.

4) Dimostrare che la grammatica al punto 3) genera un linguaggio non regolare.
(Suggerimento: osserva che tutte le stringhe del tipo $(^n \text{ true })^n$ appartengono a questo linguaggio).

5) Rimuovere la ricorsione sinistra nella grammatica prodotta al punto 3).

6) Verificare che la grammatica prodotta al punto 5) è LL(1).

7) Costruire la tabella di parsing LL(1) per tale grammatica.

8) Considerare la grammatica al punto 5) e produrne una equivalente in cui sono state rimosse le produzioni epsilon e quelle unitarie.

9) Considerare la grammatica al punto 5). Costruire per essa l'automa LR(0).

10) Verificare che la grammatica al punto 5) è SLR(1), ma non LR(0).

$$1) \text{Var} = \{a\} \quad \text{store} = \{\sigma \mid \sigma : \text{Var} \rightarrow \{\text{true}, \text{false}\}\}$$

$$\sigma_1 = \{(a, \text{true})\} \quad \sigma_2 = \{(a, \text{false})\}$$

$$\Gamma = \{\langle B, \sigma \rangle \mid B \in \text{Bexp}, \sigma \in \text{store}\}$$

$$\mathcal{I} = \{ \langle \text{true}, \sigma_1 \rangle, \langle \text{true}, \sigma_2 \rangle, \langle \text{false}, \sigma_1 \rangle, \langle \text{false}, \sigma_2 \rangle \}$$

$\rightarrow \subseteq \Gamma \times \Gamma$ è la più piccola relazione generata dalle seguenti regole

$$\frac{}{\langle a, \sigma \rangle \rightarrow \langle \sigma(a), \sigma \rangle}$$

$$\frac{}{\langle B, \sigma \rangle \rightarrow \langle B', \sigma \rangle}$$

$$\frac{}{\langle \sim B, \sigma \rangle \rightarrow \langle \sim B', \sigma \rangle}$$

$$\frac{}{\langle \text{true}, \sigma \rangle \rightarrow \langle \text{false}, \sigma \rangle}$$

$$\frac{}{\langle \text{false}, \sigma \rangle \rightarrow \langle \text{true}, \sigma \rangle}$$

$$\frac{}{\langle B_1, \sigma \rangle \rightarrow \langle B'_1, \sigma \rangle}$$

$$\frac{}{\langle B_1 \text{ and } B_2, \sigma \rangle \rightarrow \langle B'_1 \text{ and } B_2, \sigma \rangle}$$

$$\frac{}{\langle \text{true and } B_2, \sigma \rangle \rightarrow \langle B_2, \sigma \rangle}$$

$$\frac{}{\langle \text{false and } B_2, \sigma \rangle \rightarrow \langle \text{false}, \sigma \rangle}$$

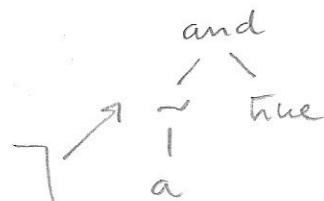
2) La grammatica è ambigua. $B ::= \text{true} \mid \text{false} \mid a \mid \sim B \mid B \text{ and } B$
Ad esempio:

$$w = \sim a \text{ and true}$$

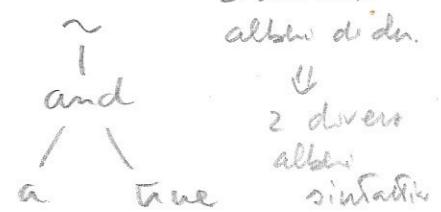
$$B \Rightarrow B \text{ and } B \Rightarrow \sim B \text{ and } B$$

$$\Rightarrow \sim a \text{ and } B \Rightarrow \sim a \text{ and true}$$

$$B \Rightarrow \sim B \Rightarrow \sim B \text{ and } B \Rightarrow \sim a \text{ and } B \Rightarrow \sim a \text{ and true}$$



Due distinte derivazioni canoniche su
2 diversi alberi di der.



2 diversi alberi sintattici

3) - "¬" lega di più di "and"

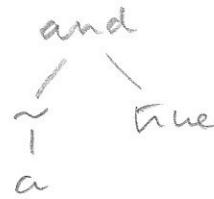
- "and" associa a sx
 \nwarrow associa a sx

$$B \rightarrow B \text{ and } T \mid T$$

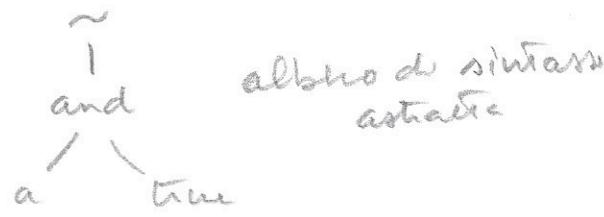
$$T \rightarrow \neg T \mid A \quad \leftarrow \text{"¬" lega più di "and"}$$

$$A \rightarrow \text{true} \mid \text{false} \mid a \mid (B)$$

$$\begin{aligned} B &\Rightarrow B \text{ and } T \Rightarrow T \text{ and } T \Rightarrow \neg T \text{ and } T \Rightarrow \neg A \text{ and } T \\ &\Rightarrow \neg a \text{ and } T \Rightarrow \neg a \text{ and } A \Rightarrow \neg a \text{ and true} \end{aligned}$$



$$\begin{aligned} B &\Rightarrow T \Rightarrow \neg T \Rightarrow \neg A \Rightarrow \neg(B) \Rightarrow \neg(B \text{ and } T) \\ &\Rightarrow \neg(T \text{ and } T) \Rightarrow \neg(A \text{ and } T) \Rightarrow \neg(a \text{ and } T) \\ &\Rightarrow \neg(a \text{ and } A) \Rightarrow \neg(a \text{ and true}) \end{aligned}$$



4) Il lvg. non è regolare.

Si prendiamo N generico

- Scegliamo $z = (^N a)^N \in L$

- Per ogni uvw tali che $z = uvw$ - $|v| \leq N - |v| \geq 1$
deve essere $v = (^i a)^i$ ($i \leq N$)

$$\Rightarrow uv^2w = (^{N+i} a)^N \notin L$$

$\Rightarrow L$ non regolare

(3)

$$B \rightarrow T B'$$

$$B' \rightarrow \text{and} \mid T B' \mid \epsilon$$

$$T \rightarrow \sim T \mid A$$

$$A \rightarrow \text{true} \mid \text{false} \mid a \mid (B)$$

6) La grammatica è LL(1)?

| | First | Follow |
|----|-------------------------|------------|
| B | ~, true, false, a, (| \$,) |
| B' | and, ε | \$,) |
| T | ~, true, false a, (| and,), \$ |
| A | true, false a, (| and,), \$ |

Caso da controllare:

$$(a) B' \rightarrow \text{and} \mid T B' \mid \epsilon$$

$$(1) \text{First}(\text{and}) = \{\text{and}\} \\ \cap \text{First}(\epsilon) = \{\epsilon\} = \emptyset$$

$$(2) \text{First}(\text{and} \mid T B') = \{\text{and}\} \\ \cap \text{Follow}(B') = \{\$\},)\} = \emptyset \\ \Rightarrow \text{OK}$$

$$(b) T \rightarrow \sim T \mid A$$

$$(1) \text{First}(\sim) = \{\sim\} \\ \cap \text{First}(A) = \{\text{true}, \text{false}, a, (\} = \emptyset$$

$$(c) A \rightarrow \text{true} \mid \text{false} \mid a \mid (B) \Rightarrow \text{OK} \\ \cap \cap \cap \cap \cap \cap$$

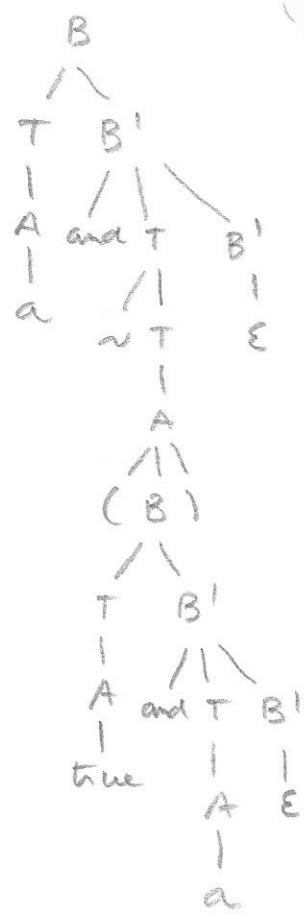
tutti i First sono diversi
 $\Rightarrow \text{OK}$

\Rightarrow la gr. è LL(1)

| | a | true | false | (|) | and | \sim | \$ |
|------|----------------------|-----------------------------|------------------------------|----------------------|---------------------------|---------------------------------------|------------------------|---------------------------|
| B | $B \rightarrow T B'$ | $B \rightarrow T B'$ | $B \rightarrow T B'$ | $B \rightarrow T B'$ | | | $B \rightarrow T B'$ | |
| B' | | | | | $B' \rightarrow \epsilon$ | $B' \rightarrow \text{and} \mid T B'$ | | $B' \rightarrow \epsilon$ |
| T | $T \rightarrow A$ | $T \rightarrow A$ | $T \rightarrow A$ | $T \rightarrow A$ | | | $T \rightarrow \sim T$ | |
| A | $A \rightarrow a$ | $A \rightarrow \text{true}$ | $A \rightarrow \text{false}$ | $A \rightarrow (B)$ | | | | |

B
 $\neg T B'$
 $\neg A B'$
 $\neg a B'$
 $\neg B'$
and $T B'$
 $T B'$
 $\neg T B'$
 $\neg \neg T B'$
 $\neg A B'$
 $\neg (B) B'$
 $\neg B) B'$
 $\neg T B') B'$
 $\neg A B') B'$
 $\neg \neg (B') B'$
 $\neg B') B'$
and $T B') B'$
 $T B') B'$
 $A B') B'$
 $\neg B') B'$
 $B') B'$
 $\neg B'$
 B'
 \neg

a and $\neg (\text{true and } a)$ B
 \neg ...
 \neg ...
a and $\neg (\text{true and } a)$ B
 and \neg ...
and $\neg (\text{true and } a)$ B
 $\neg (\text{true and } a)$ \$
 \neg (\$
 \neg (true and a) \$
 \neg (\$
 \neg true ...
 \neg true and a) \$
 \neg true ...
 \neg true ...
 \neg true and a) \$
 \neg and a) \$
 \neg a) \$
 \neg a) \$
 \neg a) \$
 \neg)\$
 \neg)\$
 \neg \$
 \neg \$
 \neg \$



8) Prese la grammatica LL(1)

$$B \rightarrow T B'$$

$$T \rightarrow \sim T \mid A$$

$$B' \rightarrow \text{and} \mid T B' \mid \epsilon$$

$$A \rightarrow \text{true} \mid \text{false} \mid a \mid (B)$$

Togliere la prod. ϵ e le prod. unitarie (in questo ordine).

$$N(G) = \{B'\}$$

Tutte le prod. che contengono B' nella parte destra vanno soppiate

$$B \rightarrow T B' \mid T \quad \leftarrow \text{nuova prod. unitaria}$$

$$B' \rightarrow \text{and} \mid T B' \mid \text{and} \mid T$$

$$T \rightarrow \sim T \mid A$$

$$A \rightarrow \text{true} \mid \text{false} \mid a \mid (B)$$

Ora togliere le 2 prod. unitarie

$$U(G) = \underbrace{\text{Id}}_{0^{\text{round}}} \cup \underbrace{\{(B, T), (T, A), (B, A)\}}_{1^{\text{round}}} \cup \underbrace{\{(B, T), (T, A), (B, A)\}}_{2^{\text{round}}}$$

$$\begin{aligned} & B \rightarrow T B' \mid \sim T \mid \text{true} \mid \text{false} \mid a \mid (B) \\ & B' \rightarrow \text{and} \mid T B' \mid \text{and} \mid T \\ & T \rightarrow \sim T \mid \text{true} \mid \text{false} \mid a \mid (B) \\ & A \rightarrow \text{true} \mid \text{false} \mid a \mid (B) \end{aligned}$$

9) Autome LR(0) per

$$(0) S \rightarrow B$$

$$(1) B \rightarrow T B'$$

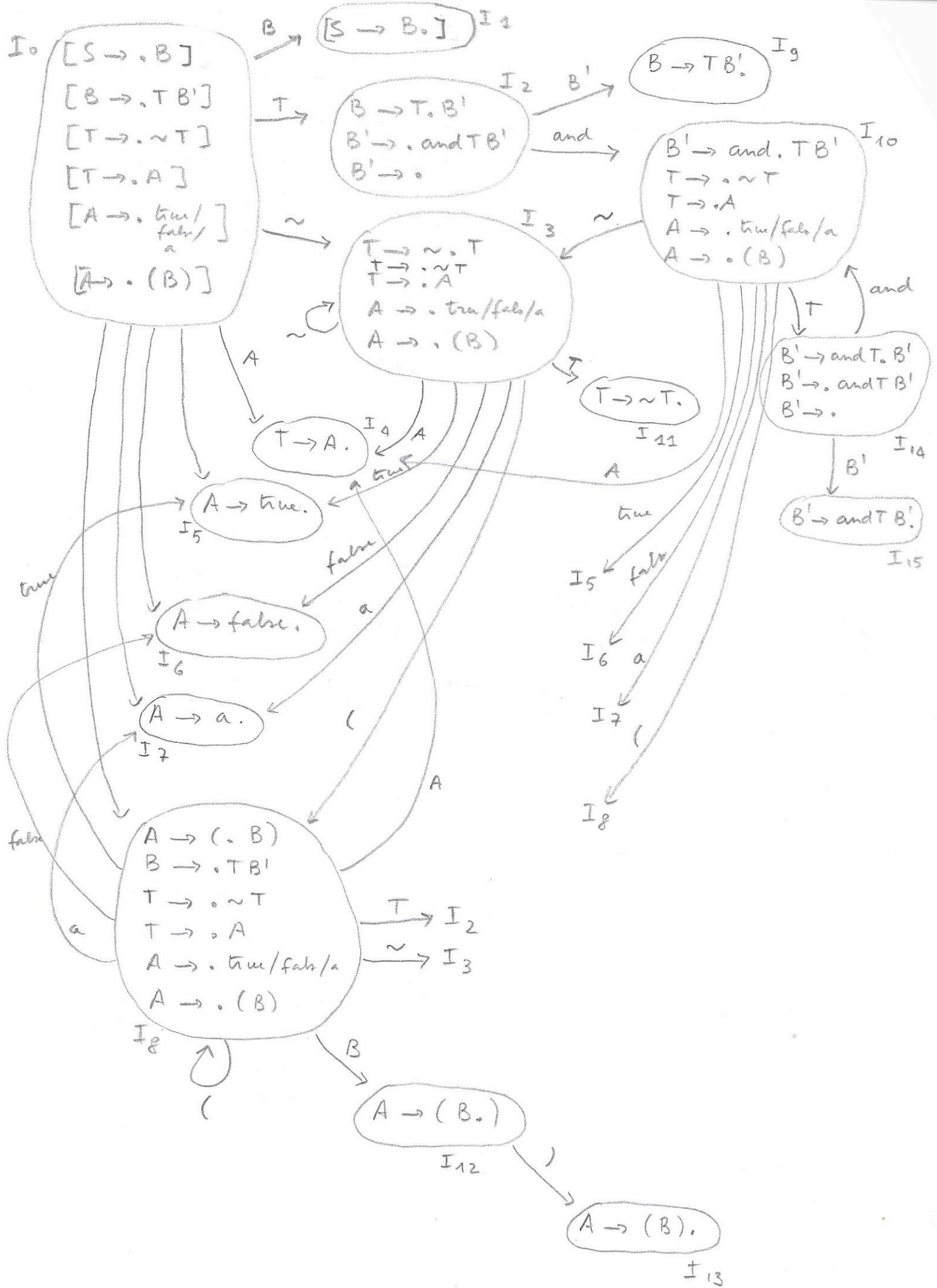
$$(2) B' \rightarrow \text{and} \mid T B'$$

$$(3) B' \rightarrow \epsilon$$

$$(4-5) T \rightarrow \sim T \mid A$$

$$(6-9) A \rightarrow \text{true} \mid \text{false} \mid a \mid (B)$$

| | First | Follow |
|------|---|---------------------|
| B | $\sim, \text{true}, \text{false}, a, ($ | $\$,)$ |
| B' | and, ϵ | $\$,)$ |
| T | $\sim, \text{true}, \text{false}, a, ($ | $\text{and}, \$,)$ |
| A | $\text{true}, \text{false}, a, ($ | $\text{and}, \$,)$ |



| | a | true | false | and | \sim | (|) | \$ | B | B' | T | A |
|-----------------|----------------|----------------|----------------|-----------------|-----------------|----------------|---|----|-----------------|-----------------|-----------------|----------------|
| I ₀ | S ₇ | S ₅ | S ₆ | | S ₃ | S ₈ | | | g ₁ | | g ₂ | g ₄ |
| I ₁ | | | | | | | | | acc | | | |
| I ₂ | | | | S ₁₀ | | | | | z ₃ | z ₃ | g ₉ | |
| I ₃ | S ₇ | S ₅ | S ₆ | | S ₃ | S ₈ | | | | | g ₁₁ | g ₄ |
| I ₄ | | | | | z ₅ | | | | z ₅ | z ₅ | | |
| I ₅ | | | | | z ₆ | | | | z ₆ | z ₆ | | |
| I ₆ | | | | | z ₇ | | | | z ₇ | z ₇ | | |
| I ₇ | | | | | z ₈ | | | | z ₈ | z ₈ | | |
| I ₈ | S ₇ | S ₅ | S ₆ | | S ₃ | S ₈ | | | | g ₁₂ | g ₂ | g ₄ |
| I ₉ | | | | | | | | | z ₁ | z ₁ | | |
| I ₁₀ | S ₇ | S ₅ | S ₆ | | S ₃ | S ₈ | | | | | g ₁₄ | g ₄ |
| I ₁₁ | | | | | z ₄ | | | | z ₄ | z ₄ | | |
| I ₁₂ | | | | | | | | | S ₁₃ | | | |
| I ₁₃ | | | | | z ₉ | | | | z ₉ | z ₉ | | |
| I ₁₄ | | | | | S ₁₀ | | | | z ₃ | z ₃ | g ₁₅ | |
| I ₁₅ | | | | | | | | | z ₂ | z ₂ | | |

$$\text{Follow}(B') = \{ \$,) \}$$

$$(3) B' \rightarrow \epsilon$$

$$(2) B' \rightarrow \text{and} T B'$$

$$\text{Follow}(A) = \{ \text{and},), \$ \}$$

$$(6-9) A \rightarrow \text{true} / \text{false} / \sim / (B)$$

$$\text{Follow}(T) = \{ \text{and},), \$ \}$$

$$(5) T \rightarrow A$$

$$(4) T \rightarrow \sim T$$

$$\text{Follow}(B) = \{), \$ \}$$

$$(1) B \rightarrow T B'$$

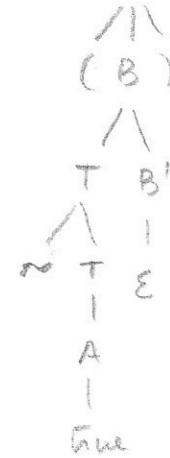
$\frac{0 \quad \epsilon}{\cancel{X} \quad \boxed{a} A}$ a and (\sim true) \$
 and (\sim true) \$ $A \rightarrow a$

$\frac{0 \quad \epsilon}{\cancel{A} \quad \boxed{T}}$ and (\sim true) \$ $T \rightarrow A$

$\frac{0 \quad T}{2 \quad T}$ and ...
 $\frac{10 \quad T \text{ and } (\sim \text{true}) \$}{8 \quad T \text{ and } (\sim \text{true}) \$}$
 $\frac{3 \quad T \text{ and } (\sim \text{true}) \$}{5 \quad T \text{ and } (\sim \text{true}) \$}$ $A \rightarrow \text{true}$



$\frac{0 \quad T \text{ and } (\sim \text{true}) \$}{2 \quad T \text{ and } (\sim \text{true}) \$}$ $T \rightarrow A$



$\frac{0 \quad T \text{ and } (\sim T) \$}{2 \quad T \text{ and } (\sim T) \$}$ $T \rightarrow \sim T$

$\frac{0 \quad T \text{ and } (\sim T) \$}{2 \quad T \text{ and } (\sim T) \$}$ $B' \rightarrow \epsilon$
 $\frac{3 \quad T \text{ and } (TB') \$}{5 \quad T \text{ and } (TB') \$}$ $B \rightarrow TB'$

$\frac{0 \quad T \text{ and } (B) \$}{2 \quad T \text{ and } (B) \$}$ $A \rightarrow (B)$
 $\frac{10 \quad T \text{ and } (B) \$}{12 \quad T \text{ and } (B) \$}$

$\frac{0 \quad T \text{ and } A \$}{2 \quad T \text{ and } A \$}$ $T \rightarrow A$

$\frac{0 \quad T \text{ and } A \$}{2 \quad T \text{ and } A \$}$
 $\frac{10 \quad T \text{ and } T_B \$}{14 \quad T \text{ and } T_B \$}$ $B' \rightarrow \epsilon$
 $\frac{15 \quad T \text{ and } TB' \$}{15 \quad T \text{ and } TB' \$}$ $B' \rightarrow \text{and } TB'$

$\frac{0 \quad TB' \$}{2 \quad TB' \$}$ $B \rightarrow TB'$

$\frac{0 \quad B}{1 \quad B}$ accept